Week 4
MATH 33A
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2.1.33 Consider the transformation $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ that rotates any vector $x$ by 45 degrees in the counterclockwise direction.
(a) Show that this is a linear transformation.
(b) Find the matrix representation of $T$.
2.2.7 Let $L$ be the line in $\mathbb{R}^{3}$ that consists of all the scalar multiplies of the vector $\left[\begin{array}{l}2 \\ 1 \\ 2\end{array}\right]$. Find the reflection of the vector $\left[\begin{array}{l}1 \\ 1 \\ 1\end{array}\right]$ about the line $L$.
2.2.18 The linear transformation $T(x)-\left[\begin{array}{cc}0.6 & 0.8 \\ 0.8 & \\ -0.6 & \end{array}\right] x$ is a reflection about a line. Find the line (in the form $y=m x+b$ ).
2.2.40 Let $P$ and $Q$ be two perpendicular lines in $\mathbb{R}^{2}$ For a vector $x$ in $\mathbb{R}^{2}$, what is $\operatorname{proj}_{P}(x)+$ $\operatorname{proj}_{Q}(x)$ ? Give this in terms of $x$. Draw a sketch to justify your answer.

